## LETTERS

## **Quantum teleportation between light and matter**

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Quantum teleportation<sup>1</sup> is an important ingredient in distributed quantum networks<sup>2</sup>, and can also serve as an elementary operation in quantum computers<sup>3</sup>. Teleportation was first demonstrated as a transfer of a quantum state of light onto another light beam<sup>4-6</sup>; later developments used optical relays<sup>7</sup> and demonstrated entanglement swapping for continuous variables<sup>8</sup>. The teleportation of a quantum state between two single material particles (trapped ions) has now also been achieved<sup>9,10</sup>. Here we demonstrate teleportation between objects of a different nature-light and matter, which respectively represent 'flying' and 'stationary' media. A quantum state encoded in a light pulse is teleported onto a macroscopic object (an atomic ensemble containing 1012 caesium atoms). Deterministic teleportation is achieved for sets of coherent states with mean photon number (n) up to a few hundred. The fidelities are 0.58  $\pm$  0.02 for n = 20 and 0.60  $\pm$  0.02 for n = 5 higher than any classical state transfer can possibly achieve<sup>11</sup>. Besides being of fundamental interest, teleportation using a macroscopic atomic ensemble is relevant for the practical implementation of a quantum repeater<sup>2</sup>. An important factor for the implementation of quantum networks is the teleportation distance between transmitter and receiver; this is 0.5 metres in the present experiment. As our experiment uses propagating light to achieve the entanglement of light and atoms required for teleportation, the present approach should be scalable to longer distances.

Quantum teleportation—a disembodied transfer of a quantum state with the help of distributed entanglement—was proposed in a seminal paper<sup>1</sup>. The generic protocol of quantum teleportation begins with the creation of a pair of entangled objects which are shared by two parties, Alice and Bob. This step establishes a quantum link between them. Alice receives an object to be teleported and performs a joint measurement on this object and her entangled object (a Bell measurement). The result of this measurement is communicated via a classical communication channel to Bob, who uses it to perform local operations on his entangled object, thus completing the process of teleportation.

In our experiment, a pair of entangled objects is created by sending a strong 'in' pulse of light (shown on the left in Fig. 1) through an atomic sample at Bob's location. As a result of the interaction between the light and the atoms, the transmitted 'out' light received by Alice's and Bob's atoms become entangled. On Alice's site the entangled pulse is mixed with the pulse to be teleported on a 50/50 beamsplitter (BS in Fig. 1). A Bell measurement in the form of homodyne measurements of the optical fields in the two output ports of the BS is carried out and the results are transferred to Bob as classical photocurrents. Bob performs spin rotations on the atoms to complete the teleportation protocol. Finally, the state of the atoms is analysed to confirm that the teleportation has been successful.

The experiment follows a recent proposal for light-to-atoms teleportation<sup>12</sup> using multimode entanglement of light with an

atomic ensemble placed in a magnetic field. We describe teleportation in the language of dimensionless canonical variables<sup>13</sup>; this provides a common description for light and atoms, and allows for a complete tomographic characterization of the states.

The atomic object is a spin-polarized gas sample of approximately  $N_{\rm at} = 10^{12}$  caesium atoms in a  $25 \times 25 \times 25$  mm paraffin-coated glass cell at around room temperature<sup>14-18</sup> placed in a homogeneous magnetic field (**B**). Atoms are initially prepared in a coherent spin state by a 4-ms circularly polarized optical pumping pulse propagating along the direction of the magnetic field, into the sublevel F = 4,  $m_F = 4$  (Fig. 1) of the ground state with the collective ensemble angular momentum  $\langle \hat{J}_x \rangle = J_x = 4N_{\rm at}$ , and the transverse projections with minimal quantum uncertainties,  $\langle \delta J_y^2 \rangle = \langle \delta J_z^2 \rangle = \frac{1}{2}J_x$ . Changing to the frame rotating at the Larmor frequency  $\Omega$  and introducing the canonical variables for the collective transverse atomic spin components<sup>12</sup>, we obtain  $\hat{X}_A = \hat{J}_v^{\rm tot}/\sqrt{J_x}$ ,  $\hat{P}_A = \hat{J}_z^{\rm tot}/\sqrt{J_x}$  which obey



Figure 1 | Experimental set-up for teleportation of light onto an atomic **ensemble.** Atoms are initially optically pumped into F = 4,  $m_F = 4$  state with a 4-ms pulse. A strong y-polarized 2-ms 'in' pulse of light is then sent through the atomic sample at Bob's location and becomes entangled with the atoms (the pulse length is around 600 km and is not shown to scale in the figure). The pulse travels 0.5 m to Alice's location, where it is mixed on a beamsplitter (BS) with the object of teleportation-a few-photon coherent pulse of light-generated by the electro-optical modulator (EOM) synchronously with the strong pulse. In the two output ports of the BS, two polarization beamsplitters (PBS) split light onto two pairs of detectors which perform a polarization homodyne measurement (a Bell measurement). The results of these measurements are combined, processed electronically, as described in the text, and sent via a classical communication channel to Bob. There they are used to complete the teleportation onto atoms by shifting the atomic collective spin state with a pulse of a radio-frequency (RF) magnetic field of 0.2-ms duration. After a delay of 0.1 ms, a second strong pulse-the verifying pulse-is sent to read out the atomic state, in order to prove the successful teleportation. Inset, relevant atomic sublevels and light modes (not to scale). The frequency difference between a weak quantum field (black arrow) and the strong entangling field (thick red arrow) is equal to the Zeeman splitting of the ground state sublevels.

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the canonical commutation relation  $[\hat{X}_A, \hat{P}_A] = i$  provided that  $J_x >> \sqrt{\langle \delta J_{y,z}^2 \rangle}, \langle J_{y,z} \rangle$ . Here  $\hat{X}_A$  and  $\hat{P}_A$  are the recipient operators in the teleportation protocol.

The light to be teleported, and the 'in' and 'out' modes (Fig. 1), are described by single mode canonical operators<sup>6,12</sup>  $\hat{Y}, \hat{Q}, \text{ and } \hat{y}^{\text{in}}, \hat{q}^{\text{in}}$  and  $\hat{y}^{\text{out}}, \hat{q}^{\text{out}}$ , respectively. These operators obeying  $[\hat{Y}, \hat{Q}] = [\hat{y}, \hat{q}] = i$  are quantum analogues of the amplitude and phase of light in classical physics, or, more precisely, of the classical quadrature phase amplitudes y, q in the decomposition of the electric field of light with the frequency  $\omega$  as  $E \propto y \cos \omega t + q \sin \omega t$  (see Methods for exact definitions). Two non-commuting variables in quantum mechanics cannot be measured without distortion. The challenge of teleportation thus consists of a faithful transfer of these not simultaneously measurable operators,  $\hat{Y}, \hat{Q}$ , onto atomic operators  $\hat{X}_A$  and  $\hat{P}_A$ . The Raman-type interaction (see Fig. 1 inset) couples the quantum  $\omega + \Omega$ sideband of the 'in' field to the Zeeman sublevels separated by the frequency  $\Omega = 322 \,\text{kHz}$ . Therefore we introduce the  $\cos \Omega t$ ,  $\sin \Omega t$ components of the light operators  $\hat{Y}_{c.s}, \hat{Q}_{c.s}$  and  $\hat{y}_{c.s}, \hat{q}_{c.s}$  (see Methods). Canonical operators for the upper sideband mode  $\hat{Y}, \hat{Q}$ can be expressed<sup>12</sup> via measurable sin( $\Omega t$ ) and cos( $\Omega t$ ) components,  $\hat{Y}_{s}, \hat{Q}_{s}, \hat{Y}_{c}, \hat{Q}_{c}$ , as  $\hat{Y} = \frac{1}{\sqrt{2}}(\hat{Y}_{s} + \hat{Q}_{c}), \hat{Q} = -\frac{1}{\sqrt{2}}(\hat{Y}_{c} - \hat{Q}_{s})$ . We first describe generation of entanglement between light and

We first describe generation of entanglement between light and atoms. The 'in' strong pulse is *y*-polarized, hence its *x*-polarized mode  $\hat{y}^{in}$ ,  $\hat{q}^{in}$  is in a vacuum state. After interaction with atoms<sup>12</sup>, the *x*-polarized 'out' mode operators  $\hat{y}^{out}$ ,  $\hat{q}^{out}$  are given by:

$$\hat{y}_{c}^{out} = \left\{ \hat{y}_{c}^{in} + \frac{\kappa^{2}}{4} \hat{q}_{s}^{in} + \frac{\kappa^{2}}{4\sqrt{3}} \nu_{s} \right\} + \frac{\kappa}{\sqrt{2}} \hat{P}_{A}^{in}, \qquad \hat{q}_{s,c}^{out} = \hat{q}_{s,c}^{in}$$

$$\hat{y}_{s}^{out} = \left\{ \hat{y}_{s}^{in} - \frac{\kappa^{2}}{4} \hat{q}_{c}^{in} - \frac{\kappa^{2}}{4\sqrt{3}} \nu_{c} \right\} - \frac{\kappa}{\sqrt{2}} \hat{X}_{A}^{in}$$

$$(1)$$

The terms in curly brackets in the equations for  $\hat{y}$  represent vacuum contributions coming from different orthogonal modes of the 'in' pulse where the canonical operators  $v_{s,c}$  represent vacuum temporal higher order canonical modes<sup>12</sup>. The terms containing  $\hat{P}_{A}^{in}$  and  $\hat{X}_{A}^{in}$  describe the imprint of the atomic state on the light via coherent forward scattering from the atomic ensemble, or, in other words, polarization rotation due to the Faraday effect<sup>14,15</sup>. The atomic spin operators are transformed by the interaction with light as follows<sup>12</sup>:

$$\hat{X}_{A}^{out} = \hat{X}_{A}^{in} + \frac{\kappa}{\sqrt{2}}\hat{q}_{c}^{in}, \quad \hat{P}_{A}^{out} = \hat{P}_{A}^{in} + \frac{\kappa}{\sqrt{2}}\hat{q}_{s}^{in}$$
 (2)

The second terms in equation (2) describe the imprint of the light state onto atoms via the dynamic Stark effect<sup>14</sup>.

The atoms–light entanglement described by equations (1) and (2) is very close<sup>12</sup>, under our experimental conditions, to the Einstein–Podolsky–Rosen entanglement optimal for quantum teleportation. The atoms–light coupling constant  $\kappa = a_1 \sqrt{N_{\text{ph}} N_{\text{at}} F \sigma \Gamma / A \Delta \propto \alpha_0}$ 

has been discussed in detail previously<sup>12,14–18</sup>. (Here  $\sigma$  is the dipole cross-section<sup>18</sup>,  $a_1$  is the vector polarizability<sup>18</sup>,  $\Gamma = 2.6 \text{ MHz}$  is the natural linewidth (HWHM) of the transition,  $N_{\rm ph} = 4 \times 10^{13}$  is the number of the *y*-polarized photons in the strong pulse,  $\Delta = 825 \text{ MHz}$  is the blue detuning of light from the atomic resonance, and  $A = 4.8 \text{ cm}^2$  is the cross-section of the atomic sample.) As in our previous experiments with the atoms–light quantum interface, strong coupling with the atomic ensemble is achieved in the region of a high resonant optical depth  $\alpha_0$ . In the experiment we choose a nearly optimal value<sup>12</sup> of  $\kappa \approx 1$  by changing  $\alpha_0 \propto N_{\rm at}$  with the temperature of the vapour. Note that another condition for strong coherent coupling is a very high  $N_{\rm ph}$  in the *y*-polarized mode.

At Alice's location (Fig. 1), the 'out' pulse is mixed on BS with the object of teleportation-a few-photon x-polarized coherent pulse with frequency  $\omega + \Omega$  generated by an electro-optical modulator (EOM). A Bell measurement of canonical variables<sup>6,12,13</sup> is performed by two sets of polarization homodyne detectors in the two output ports of BS (Fig. 1). Homodyne detection followed by the normalization to the vacuum (shot) noise of light<sup>6</sup> is a standard method for measuring canonical variables of light. In our experiment, the strong y-polarized pulse, besides driving the entangling interaction, also plays the role of a local oscillator for the homodyne detection. The variables in phase with the strong pulse  $\hat{y}_{c,s} = \frac{1}{\sqrt{2}} (\hat{y}_{c,s}^{out} + \hat{Y}_{c,s})$  are measured via a measurement of the Stokes parameter  $\hat{S}_2$  in one output of BS, whereas the out-of-phase components  $\hat{q}_{c,s} = \frac{1}{\sqrt{2}} (\hat{q}_{c,s}^{out} \hat{Q}_{c,s}$ ) are measured via the Stokes parameter  $\hat{S}_3$  in the other arm (see Methods). The  $sin(\Omega t)$  and  $cos(\Omega t)$  components are measured by processing photocurrents with lock-in amplifiers. The Bell measurement of operators  $\hat{y}_{c,s}$  and  $\hat{q}_{c,s}$  yields four results,  $y_{c,s}$  and  $q_{c,s}$ . Operationally, these values are properly normalized integrals of corresponding photocurrents over the pulse duration (see Methods). As shown in Fig. 1, the photocurrents are combined to yield two feedback signals proportional to  $y_s - q_c$  and  $y_c + q_s$  which are sent from Alice to Bob. Auxiliary magnetic field pulses14,17 with frequency  $\Omega$  and amplitudes proportional to the feedback signals are applied to the atoms, so that the collective atomic spin variables at Bob's site are shifted to become:

$$\hat{X}_{A}^{\text{rete}} = \hat{X}_{A}^{\text{out}} + g_{X}(y_{s} - q_{c}) = \hat{X}_{A}^{\text{out}} + \frac{1}{\sqrt{2}}g_{X}(\hat{y}_{s}^{\text{out}} - \hat{q}_{c}^{\text{out}}) + g_{X}\hat{Y}$$

$$\hat{P}_{A}^{\text{rete}} = \hat{P}_{A}^{\text{out}} - g_{P}(y_{c} + q_{s}) = \hat{P}_{A}^{\text{out}} - \frac{1}{\sqrt{2}}g_{P}(\hat{y}_{c}^{\text{out}} + \hat{q}_{s}^{\text{out}}) + g_{P}\hat{Q}$$
(3)

where  $g_{X,P}$  are the feedback gains. This step completes the teleportation protocol, as the light operators  $\hat{Y}, \hat{Q}$  are now transferred onto atomic operators  $\hat{X}_{A}^{\text{tele}}, \hat{P}_{A}^{\text{tele}}$ , and all other terms in equation (3) can be made small with a suitable choice of  $\kappa$  and g.

To prove that we have performed the quantum teleportation, we determine the fidelity of the teleportation. Towards this end, we send a second—verifying—strong pulse of *y*-polarized light through the

Figure 2 | Raw experimental data for a series of teleportation runs. a, Calibration of the teleportation feedback gain. Verifying pulse canonical variable  $y_c^{\text{ver}}$ versus the input pulse canonical variable Q for 10,000 teleportation runs. All dimensionless canonical variables are normalized so that their variance for a vacuum state is 1/2. The coherent input state used in the plot has a mean photon number of  $\bar{n} \approx 500$ , and is slowly modulated in phase during this measurement. The straight line fit is used for calibration of the feedback gain (see comments in the text). b, An example of data from which the atomic state variances after the teleportation are determined. Two canonical variables of the verifying pulse,  $y_c^{ver}$  and  $y_s^{ver}$ , are plotted for an input state with  $\bar{n} = 5$  and a fixed phase. The dashed lines indicate twice the standard deviation intervals  $2\sqrt{Var(y_{c,s}^{ver})}$  which are used to determine the atomic state variances as discussed in the text.



atomic ensemble after the teleportation is completed. From this measurement we reconstruct the atomic operators  $\hat{X}_A^{\text{tele}}$  and  $\hat{P}_A^{\text{tele}}$ . The fidelity is the overlap of the input state and the teleported state averaged over the input state distribution<sup>12,14,17</sup>. The classical benchmark fidelity which has to be exceeded in order to claim the success of quantum teleportation is known<sup>11</sup> for a gaussian distribution of coherent states with the width corresponding to the mean photon number  $\langle n \rangle$  centred at zero. The experimental fidelity for such distribution can be found as<sup>6,18</sup>:

$$F_n = \frac{2}{\sqrt{\left(2\langle n\rangle(1-g_X)^2 + 1 + 2\sigma_X^2\right)\left(2\langle n\rangle(1-g_P)^2 + 1 + 2\sigma_P^2\right)}}$$

The gains are defined from the mean values of atomic and light operators:  $\bar{X}_A^{\text{tele}} = g_X \bar{Y}$ ,  $\bar{P}_P^{\text{tele}} = g_P \bar{Q}$ .  $\sigma_X^2$ ,  $\sigma_P^2$  are the variances for the final gaussian state of the atoms.

The mean values for the input light operators are determined from the results of the Bell measurement:  $\bar{y}_s - \bar{q}_c = \bar{Y}$  and  $\bar{y}_c + \bar{q}_s = \bar{Q}$ . The mean values and the variances of the atomic operators are determined from the verifying pulse measurements. Using equations (1) and (3) and the input-output beamsplitter relations<sup>12</sup>, we can link the measurement of the verifying pulse on the  $S_2$  detector to the atomic mean values:  $\bar{y}_c^{\text{ver}} = \frac{\kappa}{2} \bar{P}_A^{\text{tele}} = \frac{g_{r\kappa}}{2} \bar{Q}$ ,  $\bar{y}_s^{\text{ver}} = \frac{\kappa}{2} \bar{X}_A^{\text{tele}} = \frac{g_{X\kappa}}{2} \bar{Y}$ . Using these expressions, we can calibrate  $g_{X,P}$ , as shown in Fig. 2a where  $\hat{y}_c^{\text{ver}}$ is plotted as a function of  $\hat{Q}$ , as the value of  $\kappa = 0.93$  is determined independently from the projection noise measurement (see Methods). From the linear fit to this distribution we find  $g_P$ , which can then be tuned to a desired value electronically. Results plotted in Fig. 2a along with similar results for the other operator  $\bar{y}_s(\bar{Y})$  present the proof of the successful classical transfer of the mean values of the quantum mechanical operators  $\hat{Y}, \hat{Q}$  of light onto atomic operators.

To verify the success of the quantum teleportation, we have to determine the variances of the two atomic operators which now contain the teleported input light operators. Figure 2b shows an example of results  $\hat{\gamma}_c^{\text{ver}}, \hat{\gamma}_s^{\text{ver}}$  for 250 teleportation runs for a fixed input state. Making use of equation (1) and the beamsplitter relations, we can directly find the atomic state variances from  $\operatorname{Var}\{\hat{y}_{s(c)}\}$  of such distribution as  $\sigma_{\chi(P)}^2 = \frac{4}{\kappa^2} [\operatorname{Var}\{\hat{y}_{s(c)}\} - \frac{\kappa^4}{48} - \frac{1}{2}]$ . The final values of  $\sigma_X^2, \sigma_P^2$  for a coherent state with a varied phase and a given  $\bar{n}$  are found as averages over 10,000 points (that is, 40 runs like in Fig. 2b). For example, for  $\bar{n} = 5$  we find  $\sigma_{\chi(P)}^2 = 1.20(1.12)$  taken at gains 0.96 and 0.95 respectively. The results of  $\sigma_{\chi,P}^2(g_{X,P})$  for a range of photon numbers  $\bar{n} = 0$ (vacuum),  $\bar{n} = 5$ , 20, 45, 180, 500 at various



Figure 3 | Tomographic reconstruction of a teleported state with  $\bar{n} = 5$  (coloured contour) versus the state corresponding to the best classical state transfer. Canonical variables plotted on horizontal axes are normalized so that their variance for a vacuum state is 1/2.

gains are summarized in a figure in the Supplementary Methods. From this we obtain  $\sigma_{X,P}^2(g_{X,P})$ , which can be inserted into the fidelity expression. For a given width of the gaussian distribution of coherent states we find the values of  $g_X$ ,  $g_P$ , and the corresponding  $\sigma_{X,P}^2(g_{X,P})$ which maximize the fidelity. We obtain the following fidelities for distributions with a width $\langle n \rangle = 2, 5, 10, 20, 200; F_2 = 0.64 \pm 0.02;$  $F_5 = 0.60 \pm 0.02; F_{10} = 0.59 \pm 0.02; F_{20} = 0.58 \pm 0.02; F_{200} =$  $0.56 \pm 0.03$ . The expression for the classical benchmark fidelity<sup>11</sup>  $F_n^{class} = \frac{\langle n \rangle + 1}{2\langle n \rangle + 1}$  gives  $F_2^{class} = 0.60; F_5^{class} = 0.545; F_{10}^{class} = 0.52;$  $F_{20}^{class} = 0.51; F_{200}^{class} = 0.50$  (see Supplementary Methods for details on the fidelity calculations). The maximal  $\langle n \rangle$  for successful teleportation is limited by small fluctuations of the classical gain, which for large  $\bar{n}$  lead to large uncontrolled displacements of the teleported state with respect to the input state, and hence to the decrease in the fidelity.

In Fig. 3 we show the tomographically reconstructed teleported state with the mean photon number  $\bar{n} = 5$ . Owing to the gaussian character of the state, the knowledge of the means and the variances of two quadrature phase operators is sufficient for the reconstruction.

Note that the atomic object onto which the teleportation is performed contains hundreds of billions of atoms. However, the number of excitations in the ensemble, of course, corresponds to the number of photons in the initial state of light. Those excitations are coherently distributed over the entire ensemble.

Having demonstrated the teleportation for gaussian states, we now address the applicability of this teleportation protocol to the teleportation of a light qubit, which is relevant for, for example, quantum computing<sup>3</sup>. In the Supplementary Notes we give the derivation of the predicted qubit fidelity,  $F_q$ , based on the performance of our teleportation protocol for coherent states. For experimentally relevant values of losses and decoherence,  $F_q = 0.72$ —higher than the best classical fidelity for a qubit of 0.67—can be predicted. In order to experimentally demonstrate such qubit teleportation, a source generating such a qubit in a temporal, spectral and spatial mode compatible with our atomic target is required. First steps towards generation of an atom-compatible qubit state of light have been recently made using atomic ensembles<sup>19–21</sup>, single atoms in a cavity<sup>22,23</sup>, and a photon subtracted squeezed state<sup>24</sup>.

In our experiment, the entanglement generation and the Bell measurement overlap in time because the duration of the strong pulse and the pulse to be teleported is 2 ms, which is much longer than the time it takes light to travel from Alice to Bob. This situation, also the case in some teleportation experiments<sup>6,8</sup>, is different, for example, from the teleportation<sup>7,9,10</sup> in which the entanglement generation and the Bell measurement are separated in time. This feature is not inherent to our teleportation scheme-indeed, in principle, a shorter strong pulse (of higher power) would generate the same entanglement on a timescale short compared to the propagation time, especially if the distance from Alice to Bob is extended to a few kilometres. The teleportation distance can be increased, and is limited only by propagation losses of light and the atomic coherence lifetime. The timing of the entanglement generation and the Bell measurement may be potentially important for future applications.

Further improvement of the present teleportation protocol can be achieved by performing more complex photocurrent processing with the same homodyne set-up. As shown in ref. 12 and in the Supplementary Notes, a fidelity of 0.93 can be achieved if such processing is combined with the use of an experimentally feasible<sup>25</sup> 6 dB squeezed strong pulse.

## **METHODS**

**Calibration and measurement techniques.** Physically, we perform measurements of the Stokes operators of light by two sets of balanced homodyne detectors (Fig. 1). The measurements on the first pulse represent the generalized Bell measurement. The same measurements on the second (verifying) pulse allow us to determine the teleported atomic state by performing quantum state

tomography. The relevant  $\cos(\Omega t)$  and  $\sin(\Omega t)$  modulation components of the Stokes operators are measured by processing the corresponding photocurrents with lock-in amplifiers. The Stokes operators of interest are  $\hat{S}_2$  (which is the difference between photon fluxes in the modes polarized at  $\pm 45^{\circ}$  to the vertical axis, and  $\hat{S}_3$  (which is the corresponding quantity for the left- and righthand circular polarizations).

Calibration of the measurement of canonical variables for light is based on measurements of the shot (vacuum) noise level. We measure the Stokes parameters for the *x*-polarization mode in a vacuum state. The linear dependence of the variance of the measured photocurrents on the optical power of the strong pulse proves that the polarization state of light is, in fact, shot (vacuum) noise limited<sup>25</sup>. All other measurements of  $\hat{S}_2$ ,  $\hat{S}_3$  are then normalized to this shot noise level, yielding the canonical variables as:

$$y_c = \frac{1}{\sqrt{2} \int_0^T d\tau \cos\left(\Omega t\right) S_2^{\text{vacuum}}(\tau)} \int_0^T d\tau \cos\left(\Omega t\right) S_2(\tau)$$

and similarly for  $q_c(S_3)$  and the sin  $(\Omega t)$  components. Since our detectors have nearly unity (better than 0.97) quantum efficiency, the Stokes operators can be operationally substituted with measured photocurrents.

Next we need to calibrate the atomic coherent (projection) noise level. Whereas balanced homodyne detection for light has become an established technique for determination of the vacuum state<sup>6</sup>, a comparable technique for atoms is a relatively recent invention. Here we utilize the same procedure as used in our previous experiments on the atoms–light quantum interface<sup>14,15</sup>. We use the fact that the vacuum (projection) noise level for collective atomic spin states in the presence of a bias magnetic field can be determined by sending a pulse of light through two identical atomic ensembles with oppositely oriented macroscopic spin orientation. We therefore insert a second atomic cell in the beam. As described in detail in ref. 15, the transmitted light state in this experiment is given by:

$$\hat{y}_{c}^{\text{out}} = \hat{y}_{c}^{\text{in}} + \frac{\kappa}{\sqrt{2}} \left( \hat{P}_{\text{atom1}} + \hat{P}_{\text{atom2}} \right) = \hat{y}_{c}^{\text{in}} + \kappa \hat{P}_{\text{tota}}$$

where  $\ddot{P}_{\rm total}$  is the spin canonical variable for the entire 2-cell atomic sample. Intuitively this equation can be understood by noting that terms proportional to  $\kappa^2$  in equation (1) cancel out for propagation through two oppositely oriented ensembles. A similar equation holds for  $\hat{\gamma}_{\rm s}^{\rm out}$  with substitution of  $\hat{X}_{\rm total}$  for  $\hat{P}_{\rm total}$ . The results for  ${\rm Var}(\hat{\gamma}_{c,s}^{\rm out})$  as a function of the number of atoms are shown in the figure in the Supplementary Methods. The fact that the points lie on a straight line, along with the independent measurement of the degree of spin polarization above 0.99, proves^{14,15,18} that we are indeed measuring the vacuum (projection) noise of the atomic ensemble.  $\kappa^2$  for different atomic numbers is then calculated from the graph (Supplementary Methods). Its values are in good agreement with the theoretical calculation^{18} according to  $\kappa = a_1 \sqrt{N_{\rm ph}N_{\rm at}F\sigma\Gamma/A\Delta}$ . In the experiment, we monitor the number of atoms by sending a weak off-resonant probe pulse along the direction x and measuring the tareaday rotation angle proportional to the collective macroscopic spin of the eleportation experiment, so that the value of  $\kappa^2$  is known at every stage.

**Decoherence and losses.** The main sources of imperfections are decoherence of the atomic state and reflection losses of light. For experimental values of the atomic decoherence and losses, the model developed in ref. 12 predicts, for example,  $F_5 = 0.66$ , which is still higher than the observed value owing to imperfections unaccounted for in the model but comparable to the obtained experimental results. Dissipation also affects the experimental state reconstruction procedure. The main effect of the light losses  $\varepsilon = 0.09$  is that it modifies  $\kappa$  into  $\kappa \sqrt{1-\epsilon}$ . However, this modified  $\kappa$  is, in fact, exactly the parameter measured in the two-cell calibration experiment described above, so no extra correction is due because of these losses. There is also a small amount of electronic noise of detectors which can be treated as an extra vacuum contribution to the input state.

**Standard deviation of the teleportation fidelity.** The standard deviation of the fidelity for  $\langle n \rangle \leq 20$  is calculated as follows:

$$SD(F) = \sqrt{\delta_{PN}^2 + \delta_{SN}^2 + \delta_{el}^2 + \delta_{\beta}^2 + \delta_{SNR}^2 + \delta_{fit}^2 + \delta_g^2} =$$
$$= 10^{-2} \sqrt{1.0^2 + 1.65^2 + 0.1^2 + 0.3^2 + 0.2^2 + 1.2^2 + 0.8^2} \approx 0.02$$

where  $\delta_{\rm PN} = 0.01$  is the contribution to the SD(*F*) due to the projection noise fluctuations including an error due to imperfect optical pumping,  $\delta_{\rm SN} = 0.017$  is the contribution due to the shot noise level uncertainty,  $\delta_{\rm el} = 0.001$  is the contribution of the electronics noise level fluctuations,  $\delta_{\beta} = 0.003$  is the uncertainty due to fluctuations in the atomic decay constant,  $\delta_{\rm SNR} = 0.002$  is the contribution of the fluctuations in the ratio of responses of two pairs of detectors,  $\delta_{\rm fit} = 0.012$  is the deviation due to the uncertainty of the quadratic fit

of the atomic noise as a function of gain, and  $\delta_g = 0.008$  is the contribution of the gain fluctuations. For  $\langle n \rangle > 20$ ,  $\delta_{\rm fit} = 0.016$ , giving SD(F)  $\approx 0.026 \approx 0.03$ .

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